

DUS

- diskrétné
- udalostné
- systémy

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S T U : :
· · · : :
· F E I :
· . . . :

SLOVENSKÁ TECHNICKÁ UNIVERZITA V BRATISLAVE

Fakulta elektrotechniky a informatiky

SLOVAK UNIVERSITY OF TECHNOLOGY IN BRATISLAVA

Faculty of Electrical Engineering and Information Technology

Semantics of PN

Sekvenčná sémantika

- sekvencia spustení

Nesekvenčná sémantika

- kroková sekvencia

- označené čiastočné usporiadanie (multimnožiny prechodov)

- procesy

- výrazy

Semantics of PN

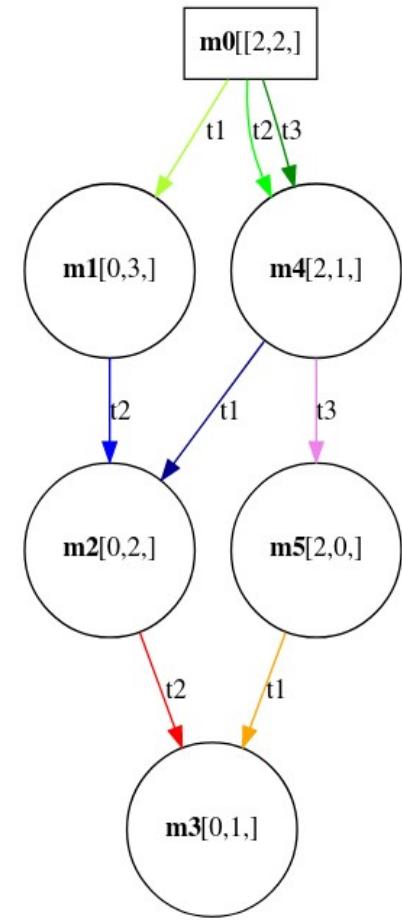
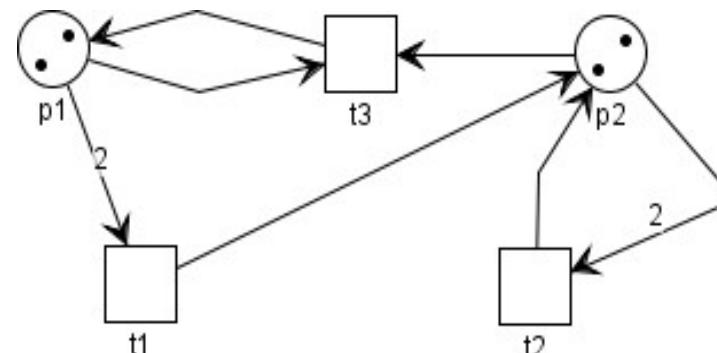
Scénar je daný sekvenciou udalostí.

Udalosť je daná spustením prechodu t v PS.

prepisovacie pravidlá scénaru z grafu dosiahnutel'nosti:

- **kauzalita** ‘;’
- **parallelizmus** ‘+’

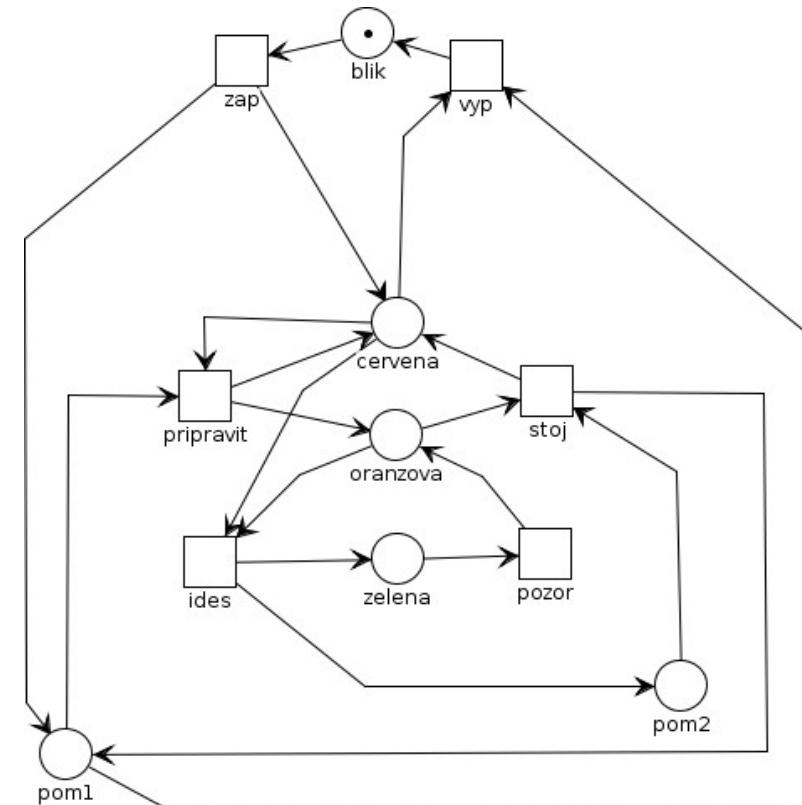
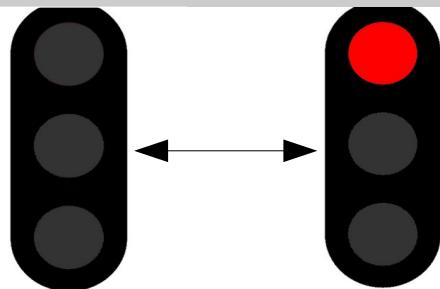
{t1;t2;t2},
{t2;t1;t2},
{t2;t3;t1},
{t3;t3;t1},
{t3;t1;t2}



$$m_0 = p1:3 \quad p2:2$$

PN reachability

stav semaforu	povolené udalosti	značkovanie
vypnutý	zap	1,0,0,0,0,0
státie (zapnutý)	vyp, prip	0,1,0,1,0,0
pripravený-volno	ides	0,1,1,0,0,0
volný	pozor	0,0,0,0,1,1
pripravený-stoj	stoj	0,0,1,0,1,0



PN

Ako vytvoriť softvér – rýchlo, lacno a v dobrej kvalite

Špecifikácia, Model driven development, Rapid system prototyping, ...

Ako vytvoriť model – rýchlo, lacno a v dobrej kvalite

(semi) automaticky

PN

Záznamy ...

Model....

Process Mining
Syntéza
Identifikácia

PN

Scénare: {F;C;A;B;D;E;F;C}, {F;E;F;E;F}, {F;C;A;B;D;C;A;B;D;C}

Stav semaforu	udalosti	značkovanie	Stav semaforu	udalosti	značkovanie	Stav semaforu	udalosti	značkovanie
?	zapnutie	??	?	zapnutie	??	?	zapnutie	??
?	pripravený	??	?	vypnutie	??	?	pripravený	??
?	ides	??	?	zapnutie	??	?	ides	??
?	pozor	??	?	vypnutie	??	?	pozor	??
?	stoj	??	?	zapnutie	??	?	stoj	??
?	vypnutie	??				?	pripravený	??
?	zapnutie	??				?	ides	??
?	pripravený	??				?	pozor	??
						?	stoj	??
						?	pripravený	??

PN Synthesis from sequence scenarios

- Metóda konečnej bázy prípustných miest
- **Metóda nesprávnych pokračovaní (WC)**
- Metóda toku značení

WC: Wrong continuations

Sekvencie v scénarii

- Gener. nerovníc z pozorovaných scénarov
- Gener. nerovníc zabraňujúce nepozorovaných scénarov
- Riešenie ...
- Optimalizácia ?

WC: Wrong continuations

Pozorované scénare: {a;b;d}, {a;c;d}

identifikácia udalostí ...

a b c d

Záznamy<id> <udalosť>:

0 a

0 b

1 a

1 c

0 d

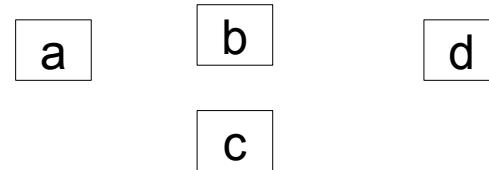
1 d

WC: Wrong continuations

Pozorované scénare: {a;b;d}, {a;c;d}

Sekvencia a;b;d:

Sekvencia a;c;d:



Záznamy<id> <udalosť>:

0 a	1 a
0 b	1 c
0 d	1 d

WC: Wrong continuations

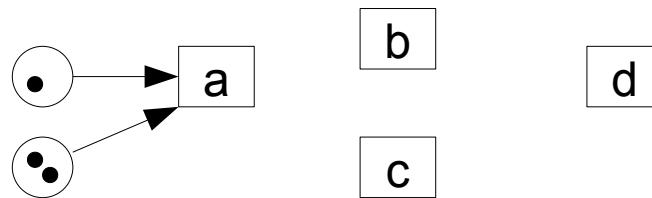
Pozorované scénare: {a;b;d}, {a;c;d}

Sekvencia a;b;d: $m \geq a_z$;

Sekvencia a;c;d: $m \geq a_z$;

$$m^T_x = m^T + C.X^T$$

$$m^T \geq I.X^T$$



$$\begin{aligned} T &= \{a, b, c, d\}; \\ X_a &= (1, 0, 0, 0) \\ I.X_a^T &= a_z \end{aligned}$$

$$m^T \geq a_z$$

WC: Wrong continuations

Pozorované scénare: {a;b;d}, {a;c;d}

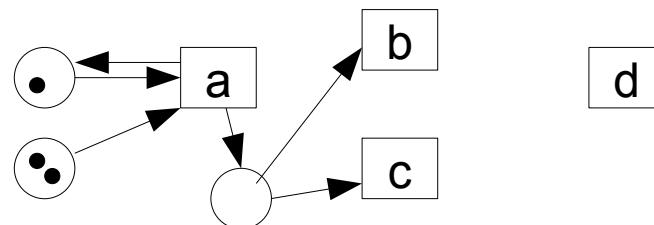
Sekvencia **a;b;d**: $m \geq a_z$; $m \geq a_z - a_d + b_z$;

Sekvencia **a;c;d**: $m \geq a_z$; $m \geq a_z - a_d + c_z$;

$$m^T_x = m^T + C.X^T$$

$$m^T_x = m^T + O.X^T - I.X^T$$

$$m^T \geq I.X^T$$



$$T = \{a, b, c, d\};$$

$$X_a = (1, 0, 0, 0); X_b = (0, 1, 0, 0); X_c = (0, 0, 1, 0)$$

$$I.X_a^T == a_z; I.X_b^T == b_z; I.X_c^T == c_z$$

$$O.X_a^T == a_d$$

$$m^T_a \geq I.X_b^T$$

$$m^T_a = m^T + O.X^T - I.X^T = m^T - a_z + a_d$$

$$m^T - a_z + a_d \geq b_z$$

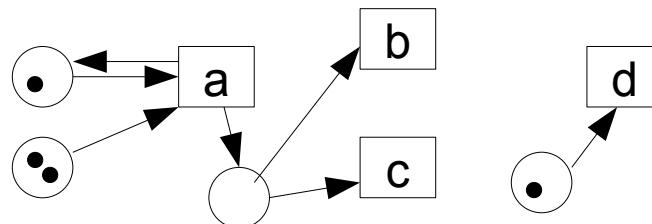
$$m^T \geq a_z - a_d + b_z$$

WC: Wrong continuations

Pozorované scénare: {a;b;d}, {a;c;d}

Sekvencia **a;b;d**: $m \geq a_z$; $m \geq a_z - a_d + b_z$; $m \geq a_z - a_d + b_z - b_d + d_z$;

Sekvencia **a;c;d**: $m \geq a_z$; $m \geq a_z - a_d + c_z$; $m \geq a_z - a_d + c_z - c_d + d_z$;



$X_a; X_b; X_c; X_d$
 $a_z \quad b_z \quad c_z \quad d_z$
 $a_d \quad b_d \quad c_d \quad d_d$

$$m^T_{ab} \geq I.X^T_d$$

$$\begin{aligned} m^T_{ab} &= m^T_a + O.X^T_b - I.X^T_b = m^T_a - b_z + b_d = \\ &= m^T - a_z + a_d + b_z - b_d \end{aligned}$$

$$m^T \geq a_z - a_d + b_z - b_d + d_d$$

WC: Wrong continuations

Pozorované scénare: {a;b;d}, {a;c;d}

Sekvencia **a;b;d**: $m \geq a_z$; $m \geq a_z - a_d + b_z$; $m \geq a_z - a_d + b_z - b_d + d_z$;

Sekvencia **a;c;d**: $m \geq a_z$; $m \geq a_z - a_d + c_z$; $m \geq a_z - a_d + c_z - c_d + d_z$;

Sekvencie **{b},{c},{d}**: $m < b_z$; $m < c_z$; $m < d_z$; d'alej...

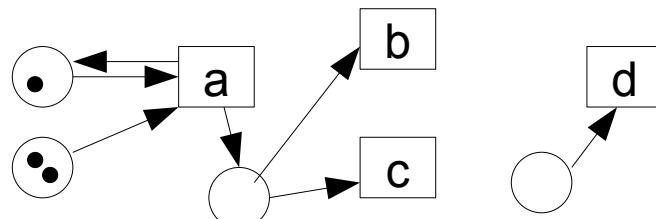
$X_a; X_b; X_c; X_d$

$a_z \quad b_z \quad c_z \quad d_z$

$a_d \quad b_d \quad c_d \quad d_d$

$m^T < I.X^T_b \quad ; \quad m^T < I.X^T_c \quad ; \quad m^T < I.X^T_d$

$m^T < b_z \dots$



WC: Wrong continuations

Pozorované scénare: {a;b;d}, {a;c;d}

Sekvencia **a;b;d**: $m \geq a_z$; $m \geq a_z - a_d + b_z$; $m \geq a_z - a_d + b_z - b_d + d_z$;

Sekvencia **a;c;d**: $m \geq a_z$; $m \geq a_z - a_d + c_z$; $m \geq a_z - a_d + c_z - c_d + d_z$;

Sekvencie **{b},{c},{d}**: $m < b_z$; $m < c_z$; $m < d_z$; d'alej

Sekvencie **{(a);d},{(a);a}**: $m < a_z - a_d + d_z$; $m < 2a_z - a_d$; ...

$$X_m = (a, b, c, d)$$

minulost

$$X_s = (a, b, c, d)$$

spustenie $\{X_a; X_b; X_c; X_d\}$

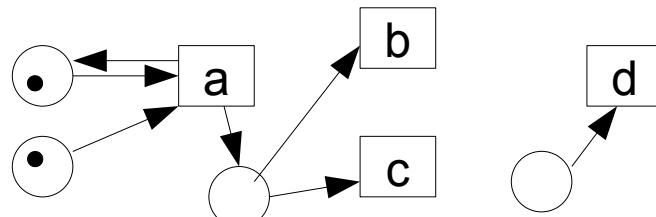
$$m^T_m \geq I.X^T_s$$

$$m^T_m = m^T + O.X^T_m - I.X^T_m = m^T \dots +/- \dots$$

$$m^T_a < I.X^T_d$$

$$m^T + O.X^T_a - I.X^T_a < I.X^T_d$$

$$m^T < a_z - a_d + d_z$$



WC: Wrong continuations

Pozorované scénare: {a;b;d}, {a;c;d}

Sekvencia a;b;d: $m \geq a_z; m \geq a_z - a_d + b_z; m \geq a_z - a_d + b_z - b_d + d_z;$

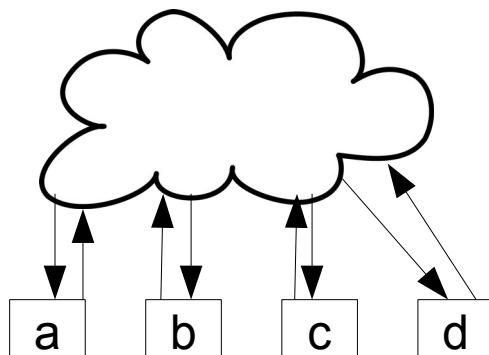
Sekvencia a;c;d: $m \geq a_z; m \geq a_z - a_d + c_z; m \geq a_z - a_d + c_z - c_d + d_z;$

Sekvencie {b},{c},{d}: $m < b_z; m < c_z; m < d_z; d\text{alej}$

Sekvencie {(a);d},{(a);a}: $m < a_z - a_d + d_z; m < 2a_z - a_d;$

Sekvencie {(ab);a},{(ab);b},{(ab);c}, {(ac);a},{(ac);b},{(ac);c}

Sekvencie {(abd);a},{(abd);b},{(abd);c},{(abd);d},
{(acd);a},{(acd);b},{(acd);c},{(acd);d}



$$X_m = (a, b, c, d);$$

minulost

$$X_s = (a, b, c, d);$$

spustenie \{X_a; X_b; X_c; X_d\}

$$m^T_m \geq I.X^T_s$$

$$m^T_m = m^T + O.X^T_m - I.X^T_m = m^T \dots +/- \dots$$

$$m^T_a < I.X^T_d$$

$$m^T + O.X^T_a - I.X^T_a < I.X^T_d$$

$$m^T < a_z - a_d + d_z$$

$$m^T_{acd} < I.X^T_a$$

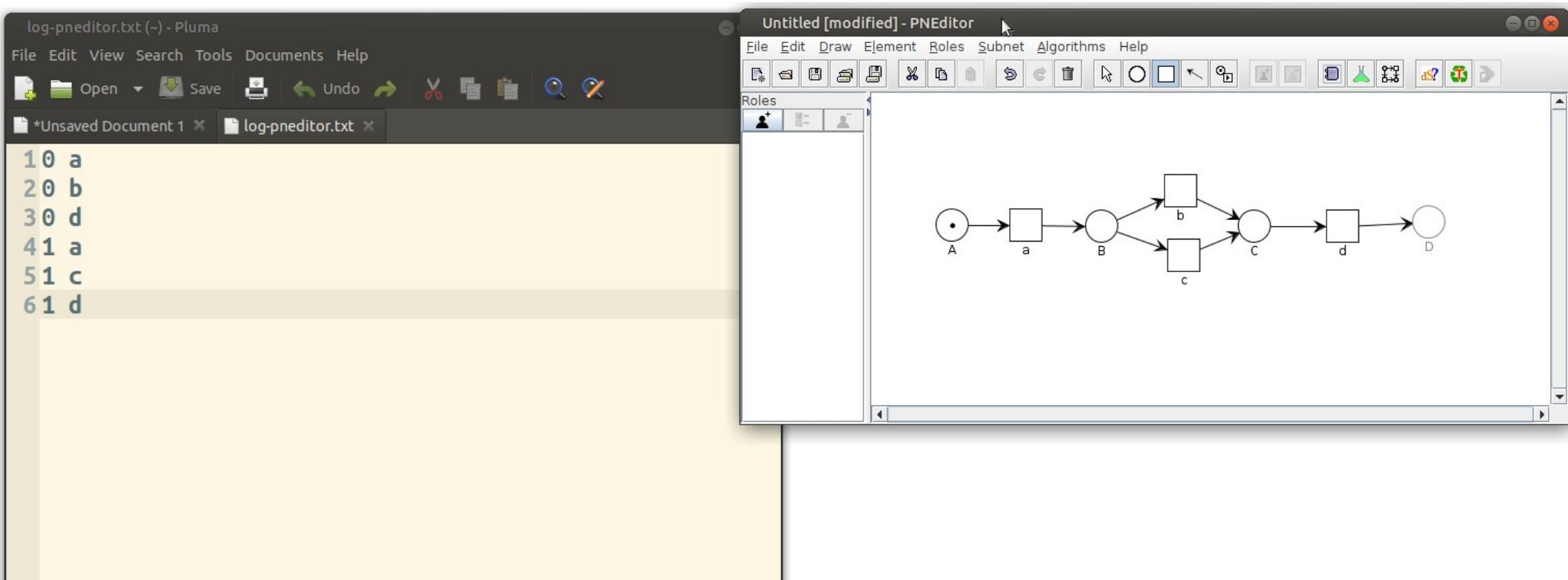
$$X_m = (1, 0, 1, 1); \quad X_s = (1, 0, 0, 0);$$

$$m^T + O.X^T_{acd} - I.X^T_{acd} < I.X^T_a$$

$$m^T < a_z - a_d + c_z - c_d + d_z - d_d + a_z$$

...

WC: Wrong continuations



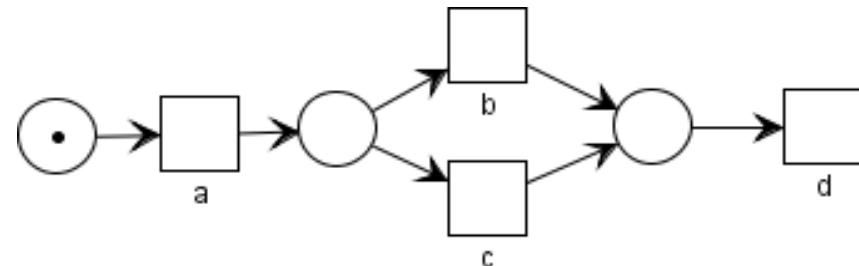
WC: Wrong continuations

5(6) nerovníc pre RC – 2 p.s.

4 prechody / udalosti, (vytv. komb. horného ohraničenia)

$3+2+6+8=19$ rovníc WC nesprávnych pokračovaní

Ekvivalencia v PN (Simple, Bisimulation, ST-bisimulation, History preserving bisimulation)



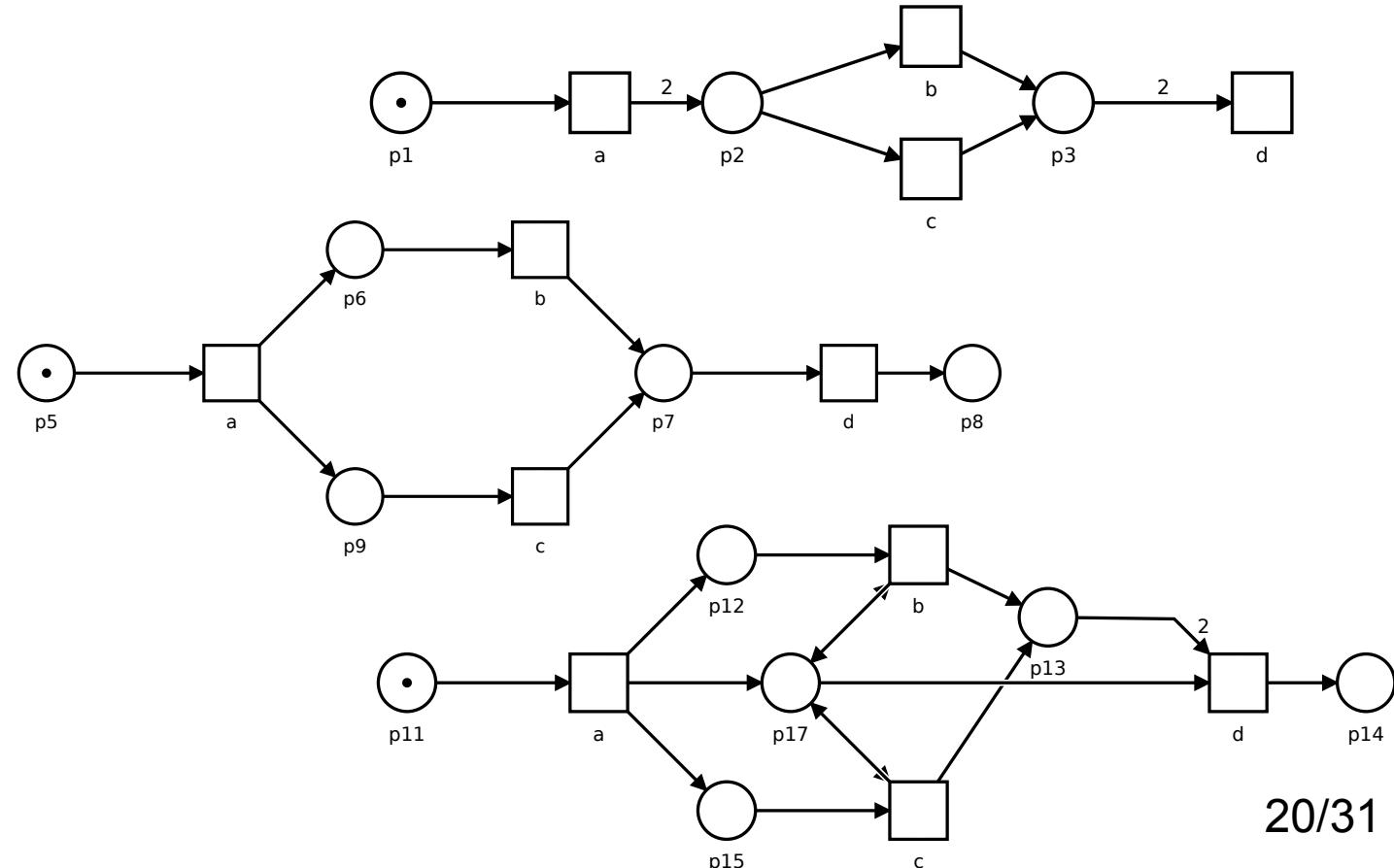
WC: Wrong continuations

Ekvivalencia v PN

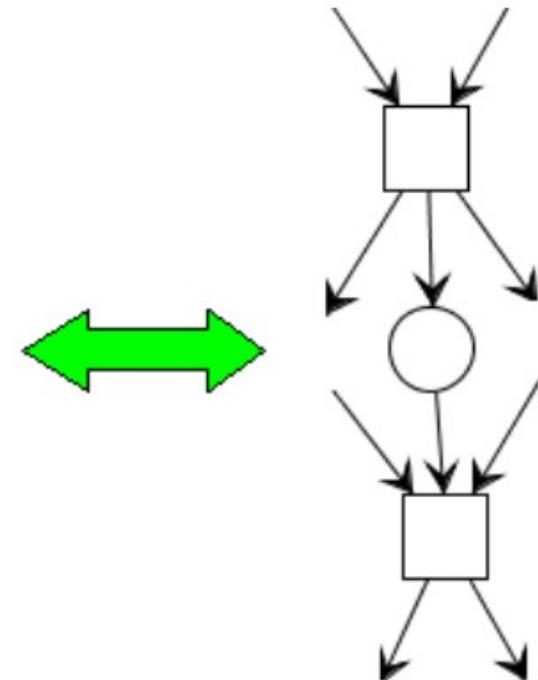
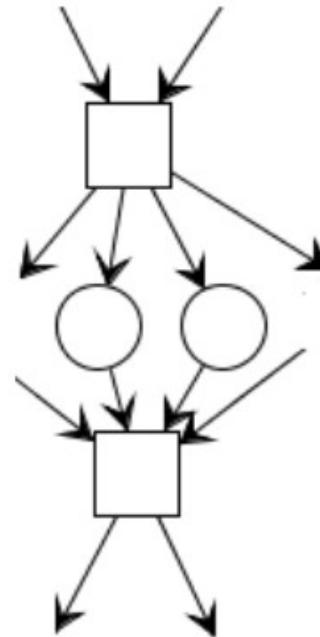
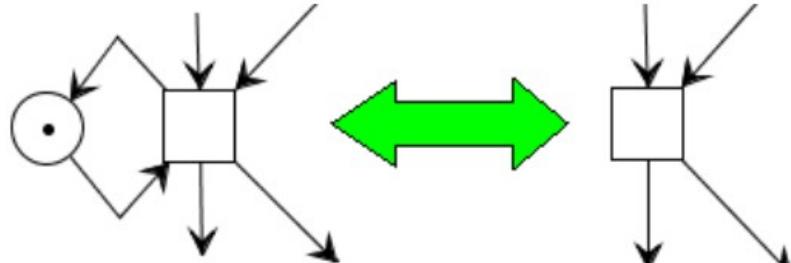
- Zober tŕacku (a)
- Zober vidličku (b)
- Zober tanier (c)
- Jedz (d)

{a;b;c;d}

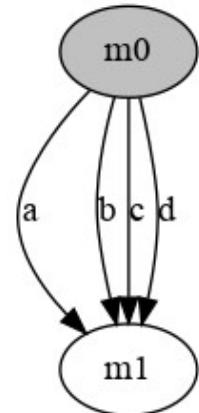
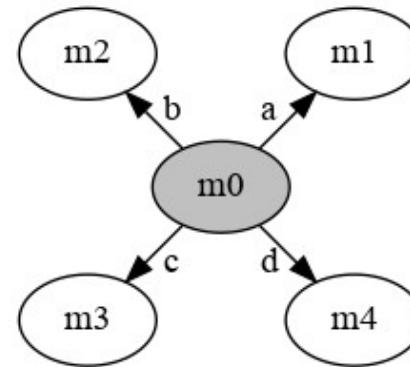
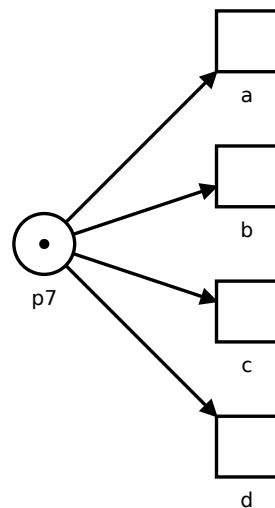
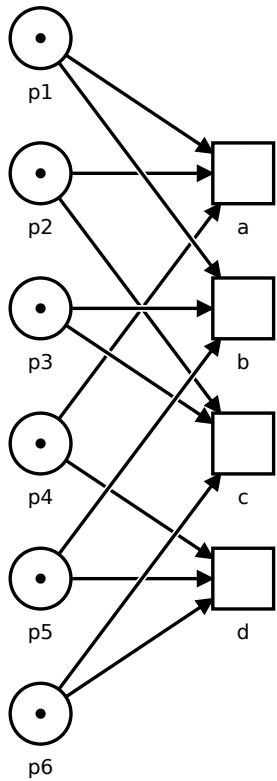
{a;c;b;d}



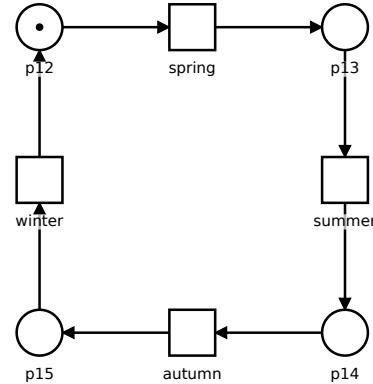
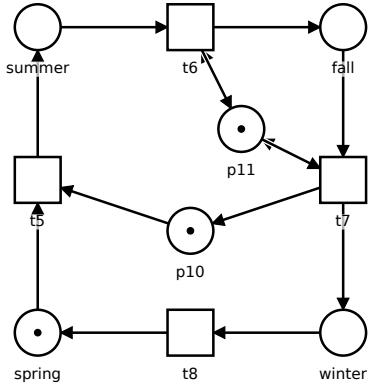
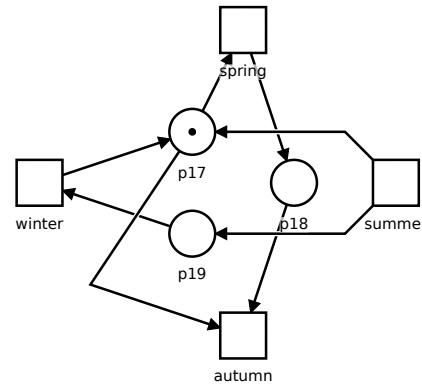
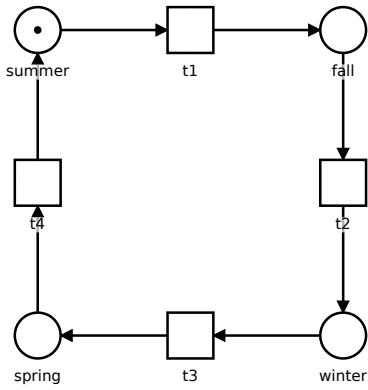
Equivalence - Reduction



Equivalences in PN



Equivalences in PN



Equivalences in PN

Ekvivalencia → izomorfizmus → bijekcia (reflex., symetr., tranzit.)

Sú grafy (f,g) izomorfné $(P?, NP?, NP\text{-}compl.?)$

László Babai (Group, graphs, algorithms: the graph isomorphism problem, 2018), kvázi-polynomial time

Marking, Trace and Language, Bisimulation

(Simple, Bisimulation, ST-bisimulation, History preserving bisimulation)

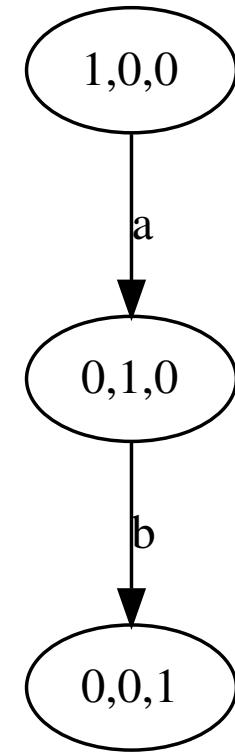
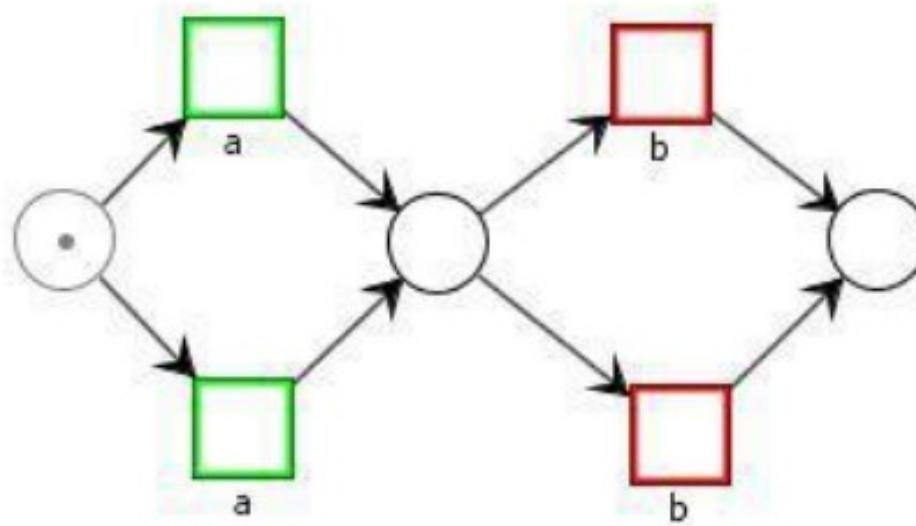
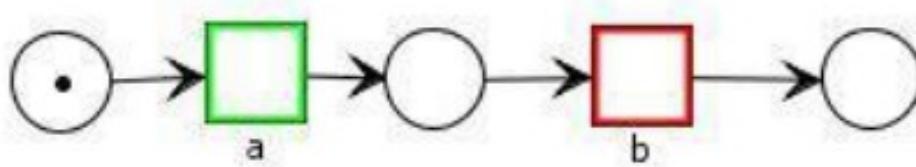
Marking Equivalence

Dve PS majúce rovnakú množinu miest sú ekvivalentné, ak majú rovnakú množinu dosiahnuteľných značení.

Problém ekvivalencie značenia je rozhodnuteľný pre ohraničené PS.

Pre neohraničené PS nevieme rozhodnúť či je siet' ekvivalentná.

Graf dosiahnutelnosti -> izomorfizmus

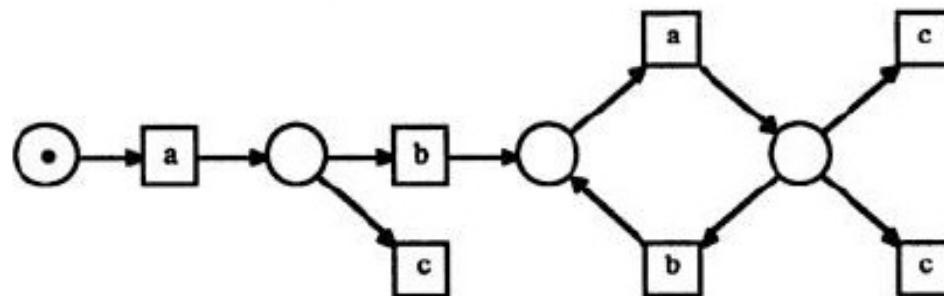
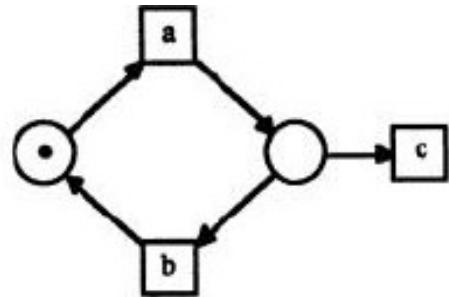


Trace and language equivalences

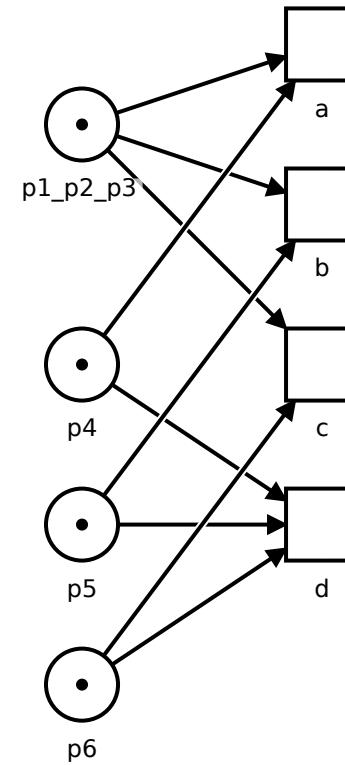
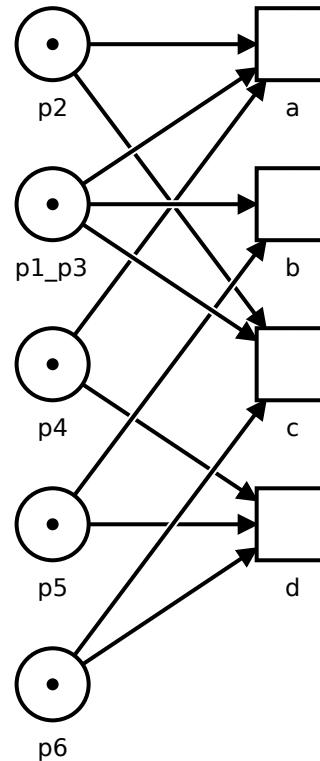
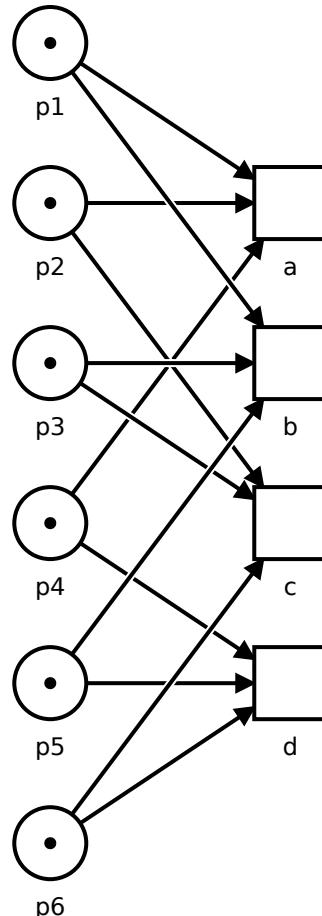
- Dve označené PS sú trace(stopovo) ekvivalentné (jazykovo ekvivalentné) ak majú rovnakú množinu stôp (jazyk).
- Nerozhodnuteľné pre viac ako 1 neohraničené miesto.

Bisimulation equivalence

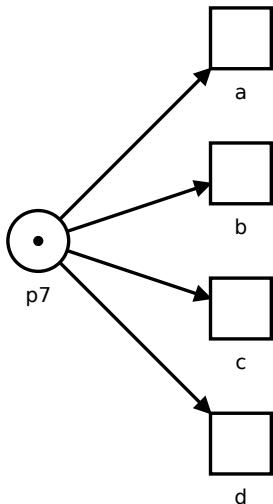
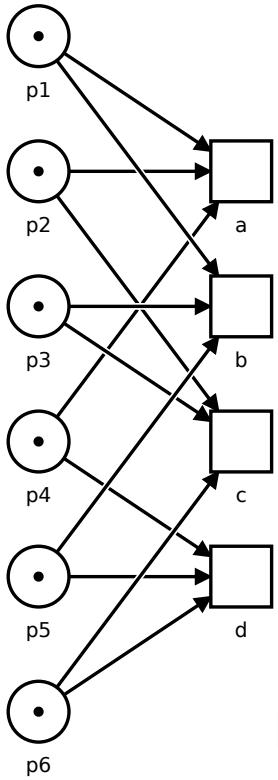
- Dve označené Petriho siete sú bisimulačne ekvivalentné, ak ich grafy dosiahnutel'nosti sú silno bisimulačne ekvivalentné.



Equivalences in PN

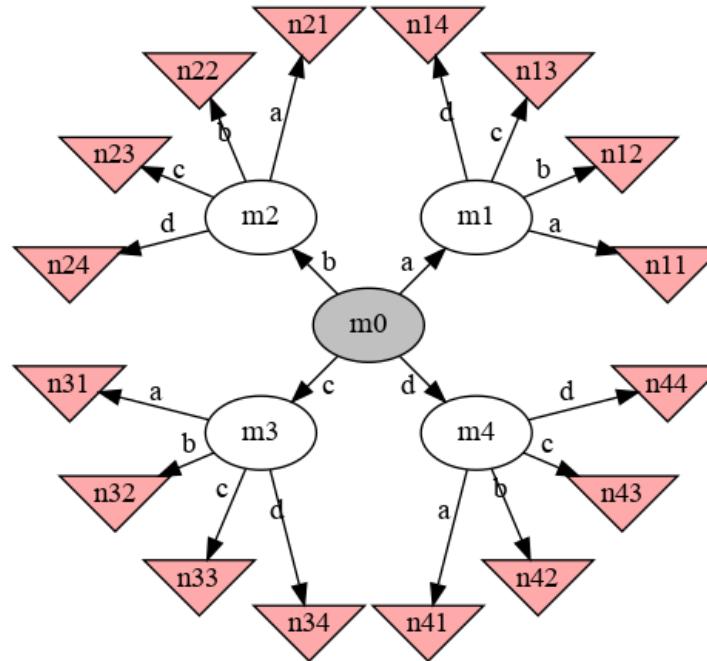


Synthesis from sequences



Problémy:

- opakovanie stavov?
- cykly, či reverzibilnosť?



- konzistentnosť?
- úplnosť?

```
digraph { rankdir=TB; rankspace=10px; node [shape=ellipse fixedsize="100x100"]; m0 [ style="filled" fillcolor=gray ]; m1 [label=m1]; m2 [label=m2]; m3 [label=m3]; m4 [label=m4]; node [shape=invtriangle]; n11 [label=n11]; n12 [label=n12]; n13 [label=n13]; n14 [label=n14]; n21 [label=n21]; n22 [label=n22]; n23 [label=n23]; n24 [label=n24]; n31 [label=n31]; n32 [label=n32]; n33 [label=n33]; n34 [label=n34]; n41 [label=n41]; n42 [label=n42]; n43 [label=n43]; n44 [label=n44]; m0->m1 [label=a]; m0->m2 [label=b]; m0->m3 [label=c]; m0->m4 [label=d]; m1->n11 [label=a]; m1->n12 [label=b]; m1->n13 [label=c]; m1->n14 [label=d]; m2->n21 [label=a]; m2->n22 [label=b]; m2->n23 [label=c]; m2->n24 [label=d]; m3->n31 [label=a]; m3->n32 [label=b]; m3->n33 [label=c]; m3->n34 [label=d]; m4->n41 [label=a]; m4->n42 [label=b]; m4->n43 [label=c]; m4->n44 [label=d]; }
```

Synthesis from sequences

- Pozorovanie existujúcich scénarov (úplných i čiastočných).
- Analýza udalostí, identifikácia.
- Generovanie nerovníc z pozorovaných scénarov.
- Generovanie nerovníc zabraňujúce scénare.
- Riešenie sústav nerovníc, tvorba miest a značiek a hrán
- Riešenie vhodnej redukcie modelu systému, ekvivalencie PS.